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# Structure determination and a vibrational study for the hexagonal elpasolite $\text{Cs}_2\text{NaGaF}_6:\text{Cr}^{3+}$

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## Abstract

Single crystals of 0.5%  $\text{Cr}^{3+}$ -doped  $\text{Cs}_2\text{NaGaF}_6$  were studied by means of x-ray diffraction and polarized Raman scattering. The crystal exhibits a unique stacking interaction, with a hexagonal structure with  $R\bar{3}m$  symmetry. Polarized Raman spectra recorded at 16 and 300 K reveal sidebands that are ascribed to the local vibrational of the  $[\text{CrF}_6]$  coordination unit, which differ markedly from those of the  $\text{Cs}_2\text{NaGaF}_6$  host lattice. The results are compared to findings for other elpasolite lattices, and the room temperature luminescence quantum yields are discussed in terms of a delicate balance between electron–phonon strength and lattice distortion.

## 1. Introduction

Numerous studies have been dedicated to the optical properties of  $\text{Cr}^{3+}$  as an impurity ion in an extended lattice [1], and more particularly in the development of solid-state lasers. The most prominent example is that of ruby, i.e.  $\text{Cr}^{3+}$  in  $\text{Al}_2\text{O}_3$ , where extensive studies of the optical properties led to the development of the first laser ever operated [2]. In the research on broadband lasers, particular attention has been focused on  $\text{Cr}^{3+}$ -doped crystalline hosts [3–7]. In this context, Cr-doped elpasolite provides an excellent model system in which to investigate crystal-field and vibronic coupling effects. In this system the electron–phonon (el-ph) interaction between the impurity centre and the host lattice is weaker than in oxide hosts, and a broad band dominates the emission spectrum. This is a fundamental property for tunable laser applications, given that the broader the emission band, the larger the tuning range.

Recently [7], we observed at 300 K a broad vibronic band that extends from the visible to the near-infrared spectral region in  $\text{Cs}_2\text{NaMF}_6:\text{Cr}^{3+}$  ( $M = \text{Ga}$  and  $\text{Al}$ ) emission spectra. As

these compounds lie near the boundary between low-field and high-field chromium complexes, the  $\text{Cr}^{3+} {}^4\text{T}_2 \rightarrow {}^4\text{A}_2$  spin-allowed transition dominates the fluorescence spectrum at room temperature, while at 77 and 4.2 K the fluorescence originates from the  ${}^2\text{E} \rightarrow {}^4\text{A}_2$  transition. Moreover the competition between the distortions in the  $t_{2g}$ ,  $e_g$ , and  $a_{1g}$  coordinates will favour radiative emission at room temperature and account for a reasonable quantum yield ( $\eta$ ) observed in the  $\text{Cr}^{3+}$ -doped fluorides.

To better understand the origin of the broadness of the emission line in these systems, it is important to understand the trend followed by the  $\text{M}^{3+}$ -F distances, due to the differences between the ionic radii,  $r_{\text{Ga}} (0.62 \text{ \AA}) > r_{\text{Cr}} (0.615 \text{ \AA}) > r_{\text{Al}} (0.53 \text{ \AA})$ , as well as the el-ph coupling strength. With this in mind, we carried out a systematic study of several  $\text{Cr}^{3+}$ -doped elpasolite lattices. Here we report on single-crystal x-ray and Raman spectroscopy (RS) measurements for 0.5%  $\text{Cr}^{3+}$ -doped  $\text{Cs}_2\text{NaGaF}_6$ . A comparison to previous work [8] allows us to obtain a correlation of the nonradiative quenching with the size of the unit cell and with the extent of the el-ph interaction in the  $\text{Cs}_2\text{NaMF}_6$  system.

## 2. Experimental details

As previously described [7], single-crystal samples with 0.5%  $\text{Cr}^{3+}$  doping were prepared by hydrothermal methods at the Institute of General and Inorganic Chemistry in Moscow.

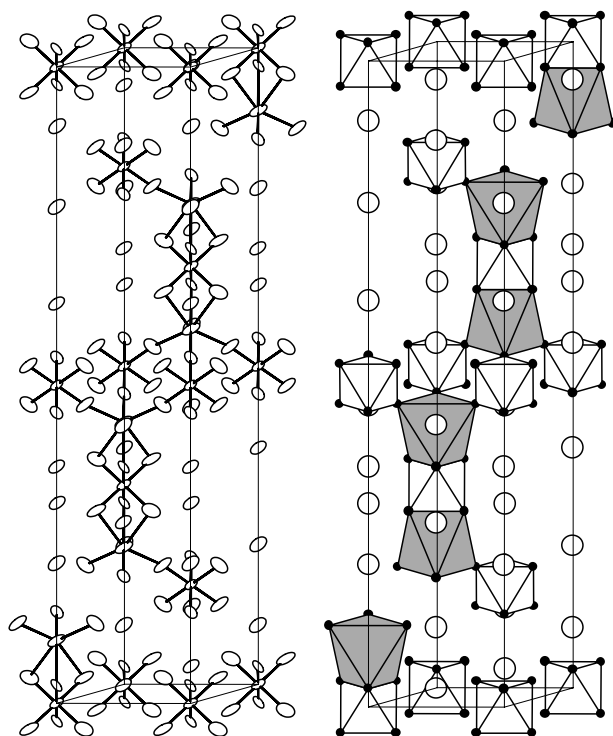
X-ray diffraction experiments were performed at room temperature on a Siemens SMART CCD area detector diffractometer. Refinements of the single-crystal structure, after applying extinction corrections, were performed using as a starting model the elpasolite structure [8] of  $\text{Cs}_2\text{NaMF}_6 \cdot \text{Cr}^{3+}$ . Also it was assumed that for a fixed Cr/Ga ratio the Cr would randomly replace some of the Ga atoms. This model was refined using the Shelx-97 package to an *R*-value of 0.018.

Polarized, single-crystal Raman scattering measurements were collected in a back-scattering configuration on a 0.5 M ARC single spectrograph ( $1800 \text{ lines mm}^{-1}/400 \text{ blaze}$ ) coupled to a Princeton Instruments LN2  $512 \times 512$  CCD array. Laser light rejection was accomplished by a Notch filter (Kaiser optical) before the entrance slit. Excitation (488.0 nm, 3.0 mW) was provided by a 10 W Spectra-Physics 2200  $\text{Ar}^+$ -ion laser. A 5 nm band pass was used to suppress the plasma lines. Polarization measurements were carried out by laser polarization rotation at a  $\lambda/4$  plate and collection of the scattered Raman intensity through a calcite polarizer. All scattering data were collected through a depolarizer prior to coupling into the spectrograph to eliminate instrumental polarization dependences. Wavenumber calibrations were carried out using argon lamps. Temperature control at  $\pm 1.0 \text{ K}$  was provided by an APD Heli-Tran cryostat controlled by a SI 9620-1 temperature controller.

## 3. Results

### 3.1. Crystal structure determination

Table 1 presents the collection parameters for the x-ray diffraction data for  $\text{Cs}_2\text{NaGaF}_6:0.5\% \text{Cr}^{3+}$ . The crystal shows a hexagonal structure with  $R\bar{3}m (D_{3d}^5)$  symmetry, with a framework composed of  $\text{GaF}_6$  octahedra that are interconnected through face- and corner-sharing  $\text{NaF}_6$  octahedra. As shown in figure 1, the structure is designated as '12 L-type', because twelve layers of Ga and Na polyhedra stack along the *c*-axis. The atomic positions and isotropic equivalent thermal parameters are given in table 2. Due to its low concentration, the Cr occupancy in the Ga sites could not be determined within experimental error. However, considering that the most important factors for substitution are the ionic radius ( $r_{\text{Ga}^{3+}} = 0.62 \text{ \AA}$ ,



**Figure 1.** An Ortep view (left) and a polyhedral representation (right) from the neutron refinement showing the connectivity between the  $\text{GaF}_6$  and the  $\text{NaF}_6$  octahedra. The white and grey polyhedra represent  $\text{GaF}_6$  and  $\text{NaF}_6$ , respectively, while the white and black atoms correspond to Ce and F. The ellipsoid probabilities were drawn at 90%. Some of the octahedra were removed for clarity.

**Table 1.** X-ray data collection parameters for  $\text{Cs}_2\text{NaGaF}_6:\text{Cr}^{3+}$ .

Temperature ( $^{\circ}\text{C}$ )	23
Crystal size (mm)	$0.5 \times 0.25 \times 0.25$
Space group	$R\bar{3}m$ (No 166)
$a$ ( $\text{\AA}$ )	6.244(1)
$c$ ( $\text{\AA}$ )	30.270(4)
$V$ ( $\text{\AA}^3$ )	1022.1(2)
$Z$	6
Radiation	X-ray, $\lambda = 0.71073 \text{ \AA}$
Data collection technique	Siemens Smart CCD
Extinction parameter	0.00557
No of reflections before averaging	3553
No of unique reflections	357
Variables	28
Function minimized	$\sum w(F_0 - F_c)^2$
Refinement type	$F^2$
$R_w(F^2)/wR2$	0.0434
$R(F)/R1$	0.0183
GOF	1.147

**Table 2.** Atomic positions and isotropic equivalent thermal parameters for Cs<sub>2</sub>NaGaF<sub>6</sub>:Cr<sup>3+</sup>.

Site symmetry	Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>U<sub>eq</sub></i>
3 <i>a</i> ( <i>m</i> )-D <sub>3d</sub>	Ga(1)	0.0	0.0	0.0	1.13
3 <i>b</i> ( <i>m</i> )-D <sub>3d</sub>	Ga(2)	0.0	0.0	0.5	0.93
6 <i>c</i> (3 <i>m</i> )-C <sub>3v</sub>	Na	0.0	0.0	0.097 68(10)	1.59
18 <i>h</i> ( <i>m</i> )-C <sub>s</sub>	F(1)	0.1408(2)	-0.1408(2)	0.962 39(8)	1.70
18 <i>h</i> ( <i>m</i> )-C <sub>s</sub>	F(2)	0.1888(2)	-0.1888(2)	0.130 85(8)	1.99
6 <i>c</i> (3 <i>m</i> )-C <sub>3v</sub>	Cs(1)	0.0	0.0	0.780 875(16)	1.81
6 <i>c</i> (3 <i>m</i> )-C <sub>3v</sub>	Cs(2)	0.0	0.0	0.628 079(15)	1.62

**Table 3.** Interatomic distances for the isostructural Cs<sub>2</sub>NaMF<sub>6</sub> elpasolites, for M = Al, Ga, Cr, and Fe.

Interatomic distance (Å)	Cs <sub>2</sub> NaAlF <sub>6</sub> :0.5Cr <sup>3+</sup> <sup>a</sup>	Cs <sub>2</sub> NaGaF <sub>6</sub> :0.5Cr <sup>3+</sup> <sup>b</sup>	Cs <sub>2</sub> NaCrF <sub>6</sub> <sup>c</sup>	Cs <sub>2</sub> NaFeF <sub>6</sub> <sup>c</sup>
M(1)-F(1)	1.813(5)	1.902(2)	1.906(5)	1.930(4)
M(2)-F(2)	1.820(5)	1.901(2)	1.913(6)	1.922(4)
Na-F(1)	2.361(1)	2.371(3)	2.370(6)	2.377(6)
Na-F(2)	2.2958(5)	2.275(3)	2.272(7)	2.266(6)

<sup>a</sup> Reference [8].<sup>b</sup> This work.<sup>c</sup> Reference [9]

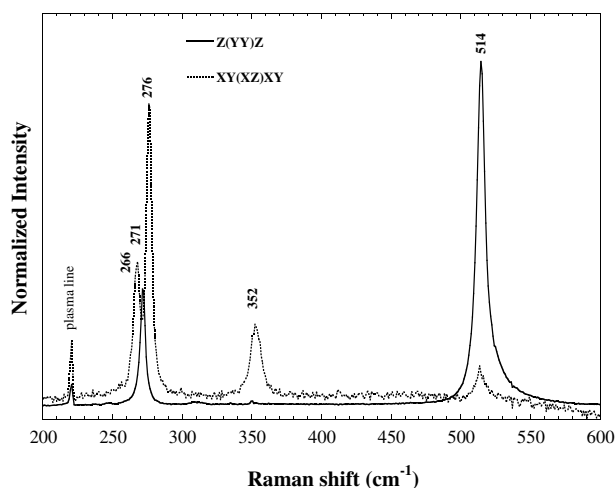
$r_{\text{Cr}^{3+}} = 0.615 \text{ \AA}$ , and  $r_{\text{Na}^+} = 0.97 \text{ \AA}$ ) and the valence (as for the Ga and Cr ions), we can argue that the Cr<sup>3+</sup> ions enter into the host substitutionally replacing the Ga<sup>3+</sup> ions, and not the Na<sup>+</sup>. Furthermore, on the basis of previous optical spectra studies on Cs<sub>2</sub>NaGaF<sub>6</sub>:Cr<sup>3+</sup> [7], we know that the Cr<sup>3+</sup> ions occupy octahedral sites, and are not randomly distributed in the lattice.

In Cs<sub>2</sub>NaGaF<sub>6</sub>, as in other hexagonal elpasolites [9–11] of  $R\bar{3}m$  (D<sub>3d</sub><sup>5</sup>) symmetry, there are two crystallographically distinct Ga positions, Ga(1) and Ga(2), which are at high-symmetry positions. The regular fluoride octahedra around the central Ga(1) ion share two trigonal faces with Na polyhedra along the *c*-axis (site 1), while the Ga(2) octahedra share all six corners with six different Na polyhedra (site 2). On the other hand, the sodium fluoride polyhedron (NaF<sub>6</sub>) is distorted, with unequal Na–F(1) and Na–F(2) distances, and the Cs atoms sit in large cavities formed by twelve fluoride atoms.

As shown in table 3, the measured bond distances in Cs<sub>2</sub>NaGaF<sub>6</sub>:Cr<sup>3+</sup> are comparable to those observed in similar structures [8, 9]. A closer inspection of the M–F interatomic distances reveals that the introduction of Cr<sup>3+</sup> in the Cs<sub>2</sub>NaMF<sub>6</sub> (M = Al, Ga) host lattice causes a bigger M<sup>3+</sup>–F bond-length variation in the aluminate system. This result is in perfect agreement with previous time-resolved emission results [7], which also indicated that the sites occupied by the Cr<sup>3+</sup> ions are more distorted in the doped Cs<sub>2</sub>NaAlF<sub>6</sub>. This larger distortion can be understood in terms of the difference in ionic radius (*r*): given that the values of  $r_{\text{Ga}^{3+}}$  and  $r_{\text{Cr}^{3+}}$  are very close,  $r_{\text{Ga}^{3+}} (0.62 \text{ \AA}) > r_{\text{Cr}^{3+}} (0.615 \text{ \AA}) > r_{\text{Al}^{3+}} (0.53 \text{ \AA})$ , it is easier to accommodate the Cr<sup>3+</sup> ion in the Cs<sub>2</sub>NaGaF<sub>6</sub> lattice than in Cs<sub>2</sub>NaAlF<sub>6</sub>.

### 3.2. Identification of the Raman-active modes

From a group theoretical analysis of the primitive cell [8], the phonons in Cs<sub>2</sub>NaAlF<sub>6</sub>:0.5Cr<sup>3+</sup> can be classified as  $7A_{1g} + 2A_{1u} + 9A_{2u} + 2A_{2g} + 9E_g + 11E_u$ , where only the A<sub>1g</sub> (*xx*, *yy*, *zz*) and E<sub>g</sub> (*xy*, *xz*, *yz*) modes are Raman active.



**Figure 2.** Polarized room temperature Raman spectra of  $\text{Cs}_2\text{NaGaF}_6:\text{Cr}^{3+}$  (0.5%) for different sample orientations. The Raman modes ( $A_{1g}$  at 271 and 514  $\text{cm}^{-1}$  and  $E_g$  at 266, 276, and 352  $\text{cm}^{-1}$ ), as well as a plasma line observed at 220  $\text{cm}^{-1}$ , are labelled in the figure. As the intensity of the  $XY(XZ)XY$  spectra is three times lower than that of the  $Z(YYZ)$  ones, the data were normalized.

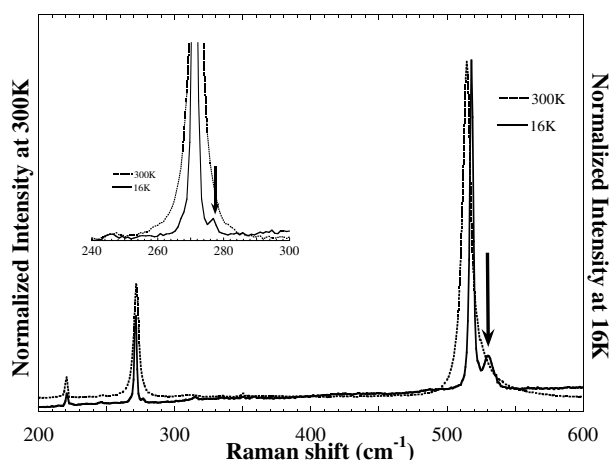
Room temperature Raman spectra are shown in figures 2(a) and (b). The measurements were performed in two different scattering geometries  $Z(YYZ)$  and  $XY(XZ)XY$ , allowing the observed Raman modes to be unambiguously determined. Polarization rules impose that for the  $Z(YYZ)$  configuration, mainly the modes of  $A_{1g}$  ( $zz$ ) symmetry should be observed, while in orientation 2,  $XY(XZ)XY$ , light is predominantly scattered by the  $E_g$  ( $xz$ ) mode.

Of the sixteen Raman-active modes, only five modes (two  $A_{1g}$ s and three  $E_g$ s) are observed between 200 and 600  $\text{cm}^{-1}$ . The Cs-ion lattice mode is expected to be observed at lower frequencies ( $<80 \text{ cm}^{-1}$ ) [12] while the mode for the Ga ion is IR active, and not observed in the Raman data. Considering that the intensity of Raman modes in an  $XY_6$  molecule normally follows the order  $I(A_{1g}) > I(E_g)$  [13], and by comparison with previous results [8, 14, 15], the observed modes were assigned. The  $A_{1g}$  modes at 271 and 514  $\text{cm}^{-1}$  arise predominantly from F-ion stretching modes in the  $D_{3d}$  factor group for the crystal. The modes at 266, 276, and 352  $\text{cm}^{-1}$  can be assigned to  $E_g$  modes corresponding to motions of the Na and F ions in the  $xy$ -plane based on the polarization data.

The sidebands of the modes located at 278 and 530  $\text{cm}^{-1}$ , whose resolution is enhanced on cooling (see figure 3), are attributed to  $[\text{CrF}_6]^{3-}$  normal modes. These values agree with the frequencies found in the literature for such complexes in different crystals [16], and also with well-defined vibrational structure observed in  $\text{Cs}_2\text{NaGaF}_6:0.5\% \text{Cr}^{3+}$  luminescence spectra [7]. Since the mode located at 530  $\text{cm}^{-1}$  lies at a frequency higher than the frequency cut-off of the system, it can be attributed to a true localized mode.

#### 4. Discussion and conclusions

The crystal structure for elpasolites  $A_2\text{BMF}_6$  depends on the radius ratio of the ions in the lattice, as described by the Goldschmidt tolerance factor [8] ( $t$ ). For  $\text{Cs}_2\text{NaGaF}_6$ ,  $t = 1.052$ , and the observed  $R\bar{3}m$  structure is predicted. On that basis, these facts become more consistent with  $\text{Cr}^{3+}$  occupation in  $\text{Ga}^{3+}$  rather than  $\text{Na}^+$  sites. The minor structural distortion of the  $[\text{GaF}_6]$  octahedra caused by the Cr-ion impurity in  $\text{Cs}_2\text{NaGaF}_6$ , as shown in the x-ray data,



**Figure 3.** Evolution as a function of temperature (300 K: dotted curve; 16 K: full curve) of the Raman spectra for the polarization  $Z(YY)Z$ . As discussed in the text, the inclusion of  $\text{Cr}^{3+}$  into the  $\text{Cs}_2\text{NaGaF}_6$  is confirmed by the 16 K Raman data, where the sidebands (at about 278 and 530  $\text{cm}^{-1}$ , and indicated by arrows) are measurable. The inset shows in more detail the sideband located at 278  $\text{cm}^{-1}$ . The slight increase of the background can be associated with luminescence effects.

is consistent with the close values calculated for the crystal-field parameters for both  $\text{Cr}^{3+}$  sites [17],  $Dq/B \approx 2.2$ . Moreover, the inclusion of  $\text{Cr}^{3+}$  into the  $\text{Cs}_2\text{NaGaF}_6$  was confirmed by the 16 K Raman data, where the sidebands (at about 278 and 530  $\text{cm}^{-1}$ ) can be associated with the  $\nu_{A_{1g}}$  modes arising from the formation of  $[\text{CrF}_6]$  coordination units.

Now we turn to the discussion of the room temperature luminescence quantum yield ( $\eta$ ) in the doped  $\text{Cr}^{3+}$  elpasolite lattices. Previous studies on  $\text{Cr}^{3+}$ -doped elpasolite systems have clearly demonstrated that lattice distortions and el-ph coupling are relevant to the multiphonon relaxation processes, and consequently the value of  $\eta$  for the system [5, 16]. In the particular case of  $\text{Cs}_2\text{NaGaF}_6:0.5\text{Cr}^{3+}$ , unlike  $\text{Cs}_2\text{NaAlF}_6:0.5\% \text{Cr}^{3+}$  and other luminescent materials [8, 18], the vibrational properties of the  $[\text{CrF}_6]^{3-}$  differ noticeably from those of the host lattice, and the large shift of 16  $\text{cm}^{-1}$  between the bulk and the local mode frequency accounts for a strong el-ph coupling. This is indeed predictable given that gallium compounds, in general, present a high degree of covalence [19]. Consequently, in  $\text{Cs}_2\text{NaGaF}_6:\text{Cr}^{3+}$  we will observe an increase in the number of relaxation pathways [7], and a lower  $\text{Cr}^{3+}$  quantum yield should be observed compared to  $\text{Cs}_2\text{NaAlF}_6:\text{Cr}^{3+}$ , i.e.  $\eta_{\text{Cs}_2\text{NaAlF}_6:\text{Cr}^{3+}} > \eta_{\text{Cs}_2\text{NaGaF}_6:\text{Cr}^{3+}}$ . This assumption is further confirmed by structural arguments [20]. Considering that the smaller the host ion, the easier it is for the  $\text{CrF}_6^-$  unit to expand upon photon excitation, the displacement of the  ${}^4\text{T}_2$  excited state [5] is smaller and more competitive with the radiative emission than the multiphonon relaxation. Therefore the room temperature quantum yield in the doped  $\text{Cr}^{3+}$  elpasolite lattices should follow the trend

$$\eta_{\text{Cs}_2\text{NaAlF}_6:\text{Cr}^{3+}} (r_{\text{Al}^{3+}} = 0.53) > \eta_{\text{Cs}_2\text{NaGaF}_6:\text{Cr}^{3+}} (r_{\text{Ga}^{3+}} = 0.62) > \eta_{\text{Cs}_2\text{NaYBr}_6:\text{Cr}^{3+}} (r_{\text{Y}^{3+}} = 0.9),$$

exactly as observed experimentally [18, 21, 22]. A value of  $\eta$  of about 0.3 and 0.4 was obtained, respectively, for  $\text{Cs}_2\text{NaGaF}_6:\text{Cr}^{3+}$  and  $\text{Cs}_2\text{NaAlF}_6:\text{Cr}^{3+}$ , while for  $\text{Cs}_2\text{NaYBr}_6:\text{Cr}^{3+}$ ,  $\eta$  is about<sup>5</sup> 0.15.

<sup>5</sup> These values were calculated considering that a room temperature luminescence quantum yield of 100% is reached at 4.2 K.

In summary, the delicate balance between lattice and charge degrees of freedom observed in the Cr-doped halide elpasolite makes this system an excellent model for use to achieve a better understanding of multiphonon relaxation processes and thus also to explore the laser potential of new systems. We are currently investigating the laser potential of Cs<sub>2</sub>NaScF<sub>6</sub>:Cr<sup>3+</sup>.

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